# FORMAL METHODS – AN INTRODUCTION



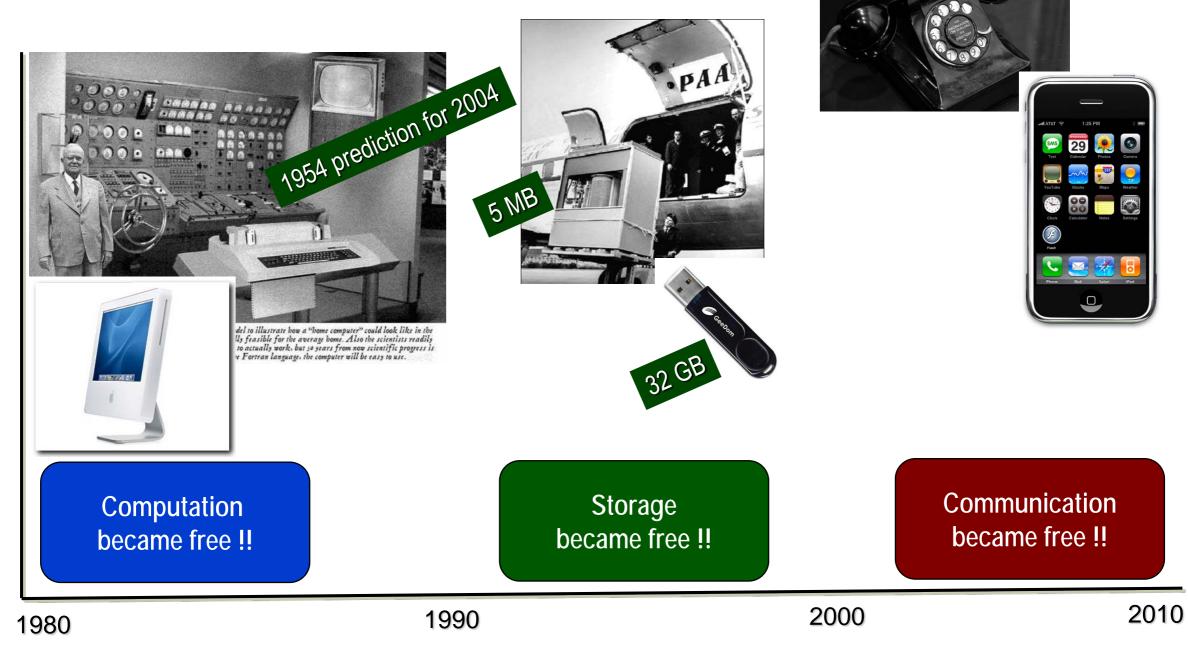




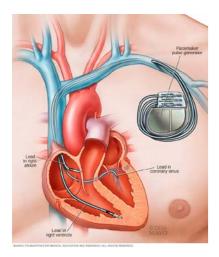
#### DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING INDIAN INSTITUTE OF TECHNOLOGY KHARAGPUR

Dr Pallab Dasgupta, Professor

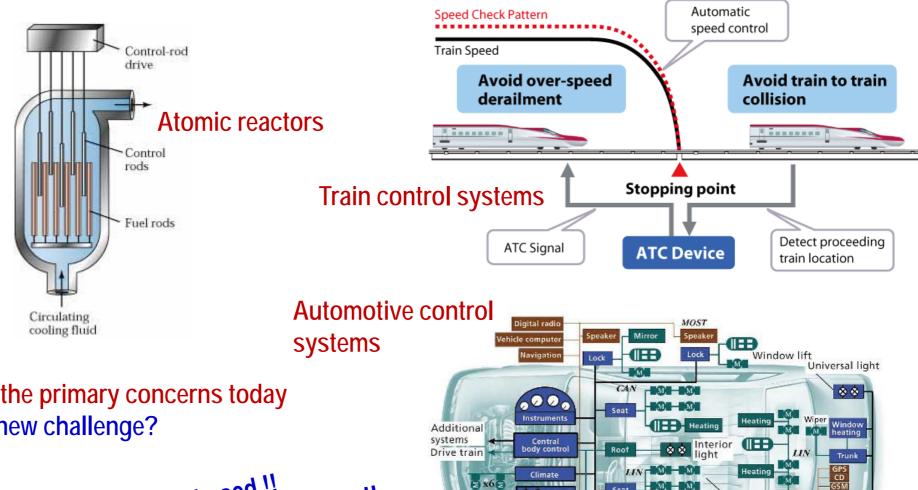
#### The Evolution of Electronic Computing



### Computing is not confined to labs anymore !!



Healthcare devices



🖄 🛞 Ligh

Controller area network

**Global Positioning System** 

Local interconnect network Media-oriented systems transport

MOST

Global System for Mobile Communications

Steering wheel

panel

CAN

GSM

Heatin

M

CAN

- Safety and security are the primary concerns today
- Why is this a relatively new challenge?



INDIAN INSTITUTE OF TECHNOLOGY KHARAGPUR

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Universal motor 😬 – Universal panel

### Safety and Computer Science

- In view of the proliferation of electronics and software in everything that we use:
  - Safety has a new meaning the electronics and software must not do things that cause my
    gadgets to harm me
  - Only Computer Science can solve the problems related to cyber safety
  - Today there are at least two people in verification for every person in design. And this is true in:
    - Design of integrated circuits
    - Design of software
    - Design of control systems

⇒ Verification experts are in high demand in modern engineering. Yet bugs continue to haunt the industry.

#### Famous incidents from software bugs



Explosion of Ariane 5, 1996 due to ".. conversion of a 64 bit integer into a 16 bit signed integer lead to an overflow ..."

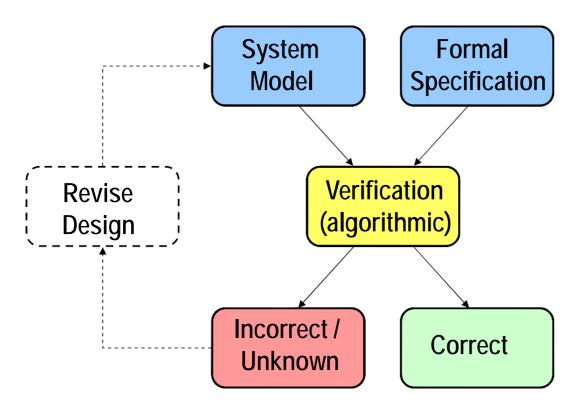


Loss of Mars Climate Orbiter, 1999 due to "...mix-up between pounds and kilogram...."

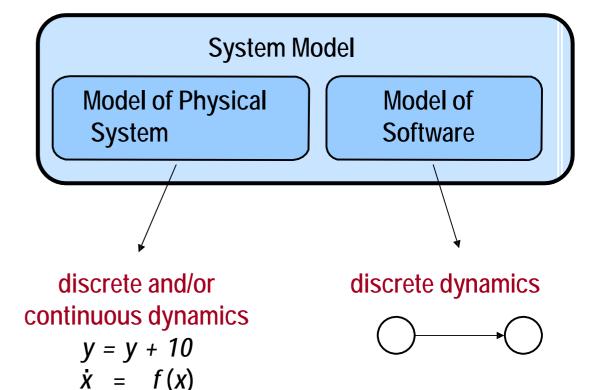


USS Yorktown died in the water, 1998 due to *"…input and Division* by '0'. *"* X / 0 = undefined…"

# Formal Methods are used to prove designs to be correct !!



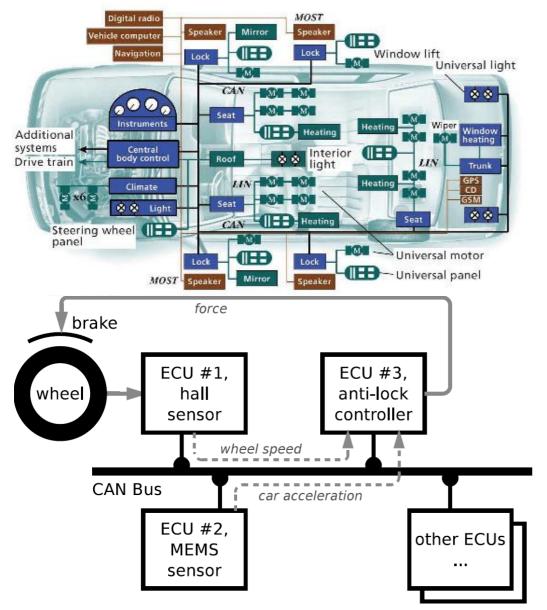
- More than 70 top scientists work in the NASA Langley formal methods group
- Top companies (Intel, IBM, Google, Microsoft, General Motors) have dedicated formal methods groups
- So does ministries of defense, atomic energy, space, etc.

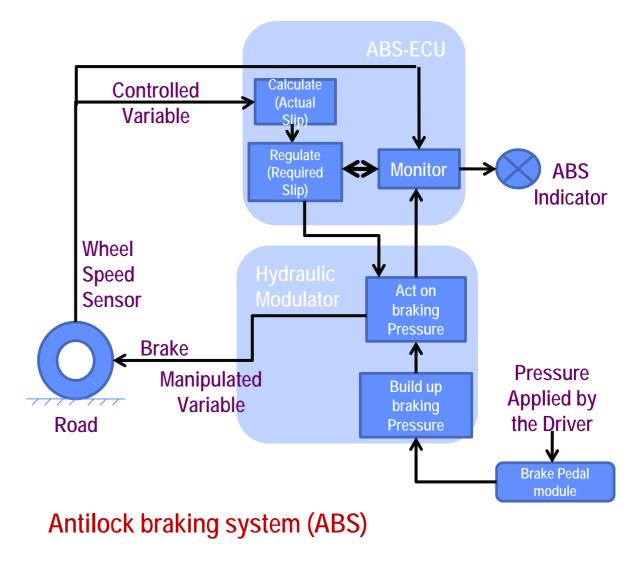


International Safety Standards recommending Formal Methods in Verification

- Aeronautics (DO-178C)
- Automotive (ISO 26262)
- Industrial process automation (IEC 61508)
- Nuclear (IEC 60880)
- Railway (EN 50128)
- Space (ECSS-Q-ST-80C)

#### **Examples of Safety Critical Systems**







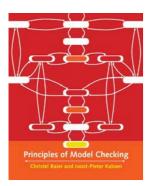
NATIONAL LOAD DESPATCH CENTER - Control room At the Top of Control Heirarchy

#### **Course Topics**

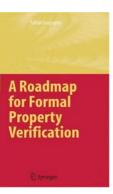
- Formal Specifications.
  - Automata over finite and infinite words, Communicating concurrent state machines, Temporal and Modal Logics, Relationship between Logic and Automata, Satisfiability, Validity and Model checking problems.
- Handling Large State Spaces.
  - Succinct representations of state spaces and their traversal, SAT and BDD-based symbolic reachability approaches, abstraction refinement approaches.
- Model Checking.
  - Temporal logic model checking, Symbolic and automata theoretic approaches.

- Formal representation of time.
  - Timed automata, Timed temporal logic, Model checking timed systems.
- Formal representation of hybrid systems.
  - Hybrid automata, Reachability problems in hybrid automata, Polyhedral approximation techniques.
- Formal analysis of programs.
  - Abstract interpretation, Predicate abstraction, Model checking software systems.
- Industrial applications of formal methods.

#### References



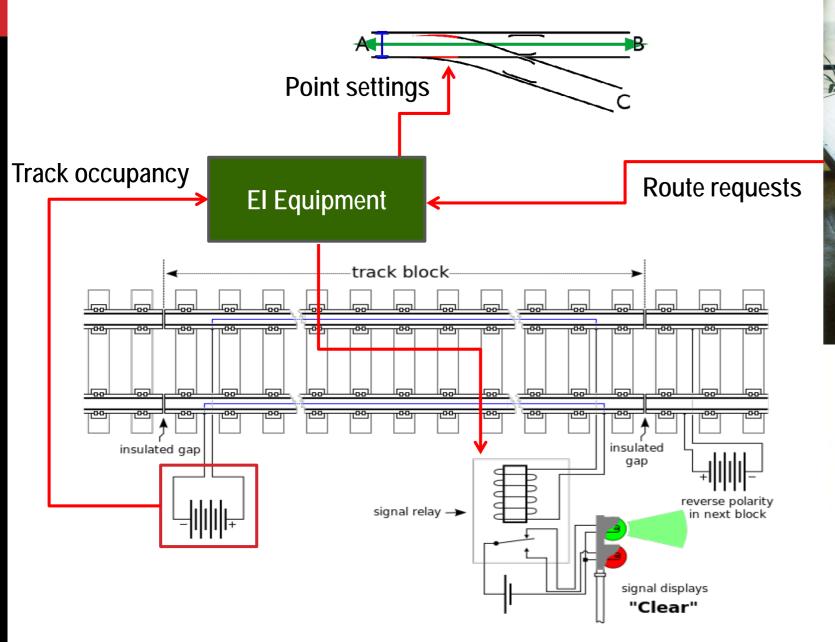
Principles of Model Checking Christel Baer, Joost-Pieter Katoen, Kim Larsen MIT Press



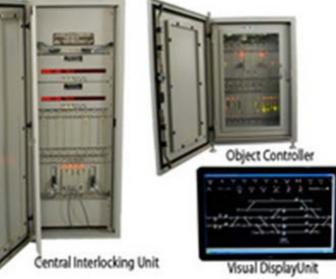
A Roadmap for Formal Property Verification Pallab Dasgupta Springer

Lectures based on this book are available in YouTube <u>https://www.youtube.com/playlist?list=PLE995EF1D8630E34F</u> A Real World Case Study

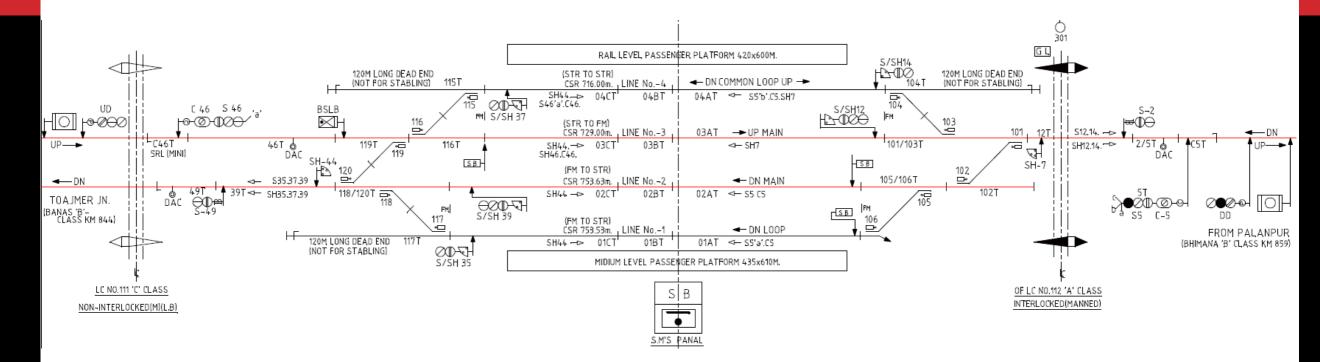
### **Electronic Interlocking in Railways**







# Life-cycle of signaling logic: Step-1 (Yard Layout)



Traditionally the layout (signal plan) is created manually

- Upgradations are reflected manually on paper
- No automatic consistency checking
- No automatic way to guarantee that upgradations in signaling plan and control table are consistent

# Life-cycle of signaling logic: Step-2 (Control Table)

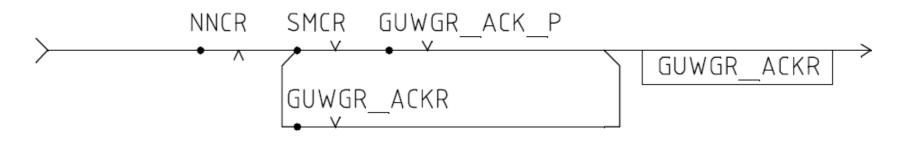
010	MGA	VEME	TN	BUT	ATION		IN RCIJTE						IN OVERL-1P						RELEASED		1	SIGNAL ASPECT		
S	FRO	DM TO	τo	GN	UN		POINTS	TRACK	SOLATION POINTS NORMAL	GATE CONTROL & OTHERS SLOTS REQUIRED NORMAL	CRANK	RANK	POINTS	TRACK	SOLATION	L STORES	CRANK	DANGER WITH	TRACK	APPROCACH	ROUTES			REMARKS
	-		-			NORMA	L REVERS	E CIRCUITS		SLOTS REQUIRED NORMAL	HANDL	NORMAL	REVERSE	CIRCUITS	POINTS		HANDLE					VELLOW	GREEN	CONTRACTOR OF THE OWNER OWNER OF THE OWNER OWN
1.	S2	BHIMANA		\$2	UM	-		2/5T	-	•		1	-	-	•	•	-	2/5T	-		(S5.C5-LN1 2.4) SH7-LN 3.4 SH12.SH14	-	-	CONTROLLED BY BHIMAN SIDE SINGLE LINE TOKENLESS B/INSTT. IN TGT POSITION WITH SSDAC.
2,	S5 b	\$3	S	55	02	105/106	101/102	2/5T 12T 101/103T 1021 105/103T, 02AT/B1/CT		301	CH-3 CH-1	117/118 115/120		118/120T 39T,		•	CH-0 CH-10	2/5T	2/5T 12T 101/103T 102T 105/106T	DEAD	S2 C5-LN2 S2 C5-LN2 SH39 SH44-LN2 C48-LN3	Š39 R OR Y OR G		. es
3,	C5	\$3	6	COGGN	02	105/106	101/102	2/5T		301	CH-3 CH-1				-				2/5T 12T 101/103T 102T 105/106T OR THRIPEM, CL.CANC,		S2 S5-LN2 S35 SH35 S37 SH37 SH39 SH44-LN1 2 3 4 C46-LN3 C46-LN3 H27 H26-LN3 H27 H26-LN3 H26-LN3 H26-LN3 H26-LN3 H26-LN3 H26-LN2 H26-LN3 H26-LN2 H26-LN3 H26-LN		1	CLEARS 60 SEC. AFTER OCC. OF C5T & REPLACED TO ON WHEN C5T IS CLEARED
4.	S5'a'	S35	5	55	01		101/102 105/106	12T 101/103T 102T	· · · · · · · · · · · · · · · · · · ·	301	CH-1 CH-3	117/118	-	1177			СН-9	2/5T	2/5T 12T 101/103T	52.C5-LN	4 W 103 104 R	S35 R	•	
-		-	-					105/106T, 01AT/ST/CT				19/120	11//118	117T, 118/120T, 39T,		-	CH-10 CH-5		102T 105/106T.	52.CS-LNI.	SHIS SHAA-LNI	S35 R OR Y	-	
5.	C5	535	S5	COGGN	01	-	101/102 105/106		-	301	СН-1 СН-3	-						6	2/5T.12T 101/103T 102T 105/106T OR THRIPEM. CU.CANC.	52.55-LNI 5H44-LN I. - (5H37.537 (5H44-LN4	1.5H35.5H37 537 2.3HC46-LN34 W 117/118 R) W 103/104R4 117/118 R) W 103/104R4	-		CLEARS 60 SEC AF I FR OCC C - C5T & REPLACED TO 'ON' WHEN C5T IS CLEARED

Traditionally the control table is created manually from the layout

- Upgradations are reflected manually on paper
- No automatic consistency checking
- No automatic way to guarantee that upgradations in control table are consistent with application logic

### Life-cycle of signaling logic: Step-3 (Application Logic)

GUWGR\_ACKR = !NNCR & ((SMCR & GUWGR\_ACK\_P) # GUWGR\_ACKR);



Traditionally the application logic is created manually from the control table

- Uses traditional relay logic (ladder network) for legacy reasons
- Lack of standardization in terms of the set of relays used to define the logic
- RDSO has been working towards a standard for Indian Railways. This will significantly help if vendors are made to comply.

### How would we verify 1000 pages of logic which looks like this?

S2GNR = S2GN\_P & IS5GNR & ISH7GNR & IS12GNR & ISH12GNR & IS14GNR & ISH14GNR & IS35GNR & ISH35GNR & IS437GNR & ISH37GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS4

S5GNR = S5GN\_P & IS2GNR & ISH7GNR & IS12GNR & ISH12GNR & IS14GNR & ISH14GNR & IS35GNR & ISH35GNR & IS37GNR & ISH37GNR & IS39GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS49

SH7GNR = SH7GN\_P & IS2GNR & IS5GNR & IS12GNR & ISH12GNR & IS14GNR & ISH14GNR & IS35GNR & ISH35GNR & IS37GNR & ISH37GNR & ISH39GNR & ISH39GNR & ISH44GNR & IS46GNR & IS46GNR & IS49GNR & IS46GNR & IS

S12GNR = S12GN\_P & IS2GNR & IS5GNR & ISH7GNR & ISH12GNR & IS14GNR & ISH14GNR & IS35GNR & ISH35GNR & IS37GNR & ISH37GNR & ISH39GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS49GNR & IS46GNR & IS49GNR & IS46GNR & IS

SH12GNR = SH12GN\_P & IS2GNR & IS5GNR & ISH7GNR & IS12GNR & IS14GNR & ISH14GNR & IS35GNR & ISH35GNR & IS437GNR & IS439GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS49GNR & IS49GNR & IS46GNR & IS49GNR & IS46GNR & IS49GNR & IS46GNR & I

S14GNR = S14GN\_P & IS2GNR & IS5GNR & ISH7GNR & IS12GNR & ISH12GNR & ISH14GNR & IS35GNR & ISH35GNR & IS37GNR & ISH37GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS4

SH14GNR = SH14GN\_P & IS2GNR & IS5GNR & ISH7GNR & IS12GNR & ISH12GNR & IS14GNR & IS35GNR & ISH35GNR & IS37GNR & ISH37GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS

S35GNR = S35GN\_P & IS2GNR & IS5GNR & ISH7GNR & IS12GNR & ISH12GNR & IS14GNR & ISH14GNR & ISH35GNR & IS37GNR & ISH37GNR & ISH39GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS49GNR & ISH35GNR & ISH35GNR & ISH35GNR & ISH37GNR & ISH39GNR & ISH39GNR & ISH44GNR & ISH44GNR & ISH46GNR & ISH

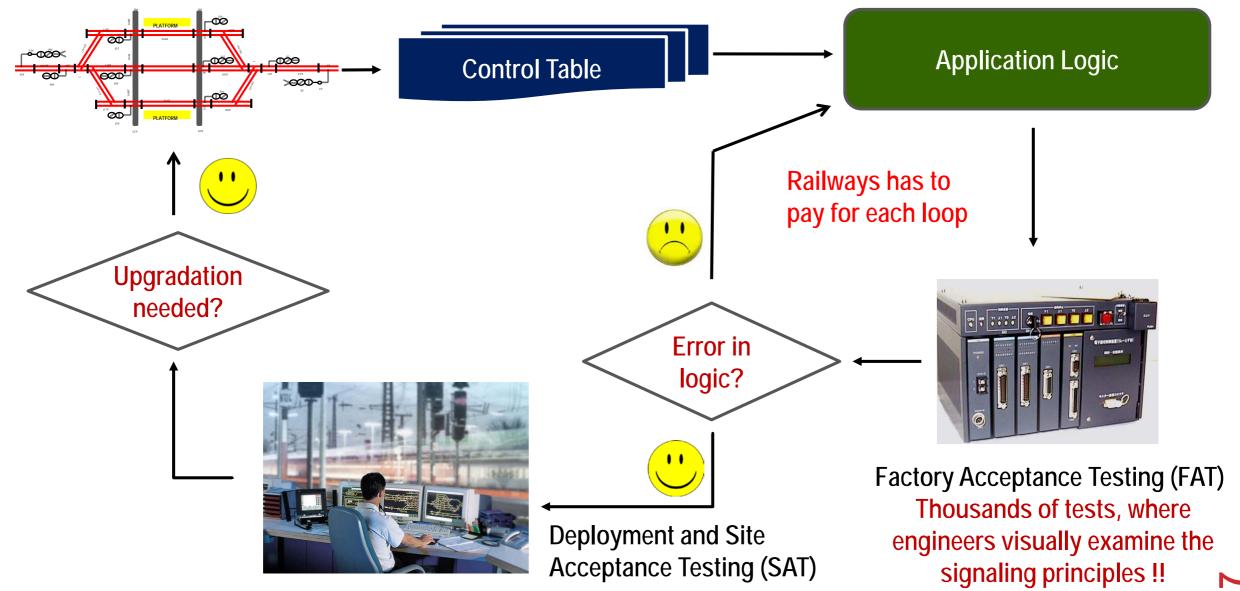
SH35GNR = SH35GN\_P & IS2GNR & IS5GNR & ISH7GNR & IS12GNR & ISH12GNR & IS14GNR & ISH14GNR & IS35GNR & IS35GNR & ISH37GNR & IS39GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS

S37GNR = S37GN\_P & IS2GNR & IS5GNR & ISH7GNR & IS12GNR & ISH12GNR & IS14GNR & ISH14GNR & IS35GNR & ISH35GNR & ISH37GNR & ISH39GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & IS49GNR & ISH35GNR & ISH35GNR & ISH35GNR & ISH39GNR & ISH39GNR & ISH44GNR & IS46GNR & IS49GNR & ISH35GNR & ISH35GNR & ISH35GNR & ISH35GNR & ISH39GNR & ISH39GNR & ISH44GNR & ISH46GNR & ISH46

SH37GNR = SH37GN\_P & !S2GNR & !S5GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !S35GNR & !S37GNR & !S39GNR & !SH39GNR & !SH44GNR & !S46GNR & !S49GNR & !S4

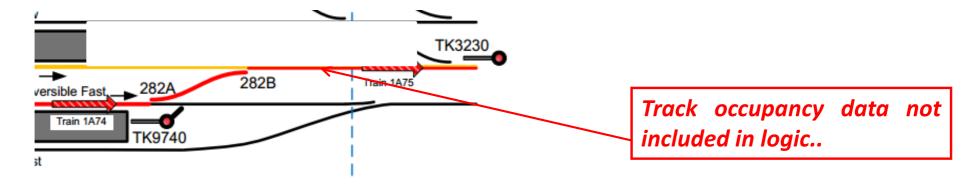
S39GNR = S39GN\_P & IS2GNR & IS5GNR & ISH7GNR & IS12GNR & IS12GNR & IS14GNR & IS14GNR & IS14GNR & IS35GNR & IS435GNR & IS435GNR & IS437GNR & IS439GNR & IS44GNR & IS46GNR & IS49GNR & IS49GNR & IS49GNR & IS46GNR & IS49GNR & IS46GNR & IS49GNR & IS46GNR & IS46GNR & IS46GNR & IS46GNR & IS49GNR & IS46GNR & IS46G

# Life-cycle for Signaling Logic



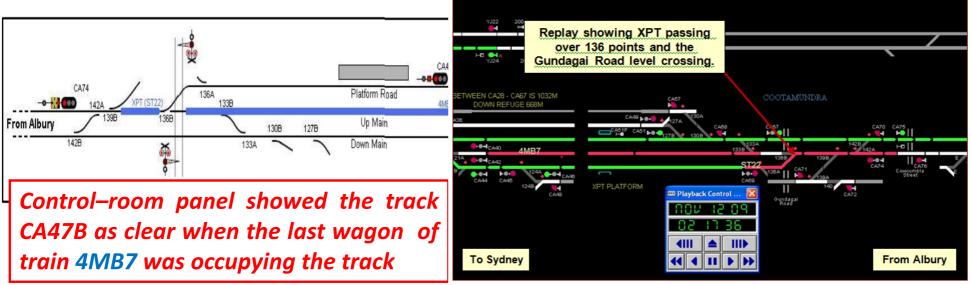
#### Milton Keynes, UK, 2008 - Cause

Formal investigations revealed, the axle-counter data was not included in the SSI logic associated with the aspect controls for signals *TK9740* and *TK3230* 



#### Cootamundra, NSW Australia, 2009 - The incident

Figure 3: Signal schematic (part) - Cootamundra Yard.



#### Railway Safety Standards recommend Formal Methods

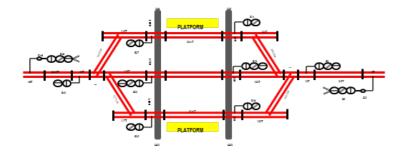
Table A.4 — Software design and implementation (clause 10)

TEC	HNIQUE/MEASURE	Ref.	SWSIL	SWSIL	SWSIL	SWSIL	SWSIL
			0	1	2	3	4
1.	Formal methods including for example CCS, CSP, HOL, LOTOS, OBJ, Temporal Logic, VDM, Z and B	B.30		R	R	HR	HR
2.	Semi-formal methods	D.7	R	HR	HR	HR	HR

Source: Page 50, EN50128: 2001

There are no guidelines in EN50128 on how such methods may be used in the context of Application Logic

### **IIT Kharagpur Contributions**



#### Layout Editor Tool

- Yard layout is created using this tool
- The tool can perform several sanity checks
- Updates can be made as and when required

	IAL	_		ROUTE		OVERLAP				Δ	Υ	AR CK			U
SL NO	ENTRY SIGNAL	EXIT SIGNAL	ROUTE	POINT NORMAL	POINT REVERSE	TRACKS	POINT NORMAL	POINT REVERSE	OVERLAP SET	CONTROLLED BY TRACK CIRCUIT	SIGNAL REPLACED BY TRACK CIRCUIT	BACK LOCKED UNTILL TRACK CIRCUIT CLEAR	LEVEL CROSSING	CRANK HANDLES	CONFLICTING ROUTES
1	S1	S5	1A	51		5T, 07T	52		OV-5	1T, 2T, 02T, 4T, 04T, 05T1, 05T2, 05T3, 05T	1T	1T, 2T, 02T, 4T	LC 1	CH1, CH2	C-1A, 4, 8A, 78A
2	S1	S3	1BD		51	3T	52		OV1-3	1T, 2T, 02T, 4T, 6T, 06T, 06T1, 06T2, 06T3, 03T	1T	1T, 2T , 02T, 4T,	LC 1	CH1, CH2	C-1B, 6, 78A
			1BM			3T, 5T, 07T		52	OV2-3			6T	LC 1		C-1B, 6, 8B, 78A, 78B, 8A, 5
3	S3	S7	3		52					3T, 5T, 07T	3Т	3T, 5T		CH2	8B, 78B, 6, C-1B
4	S5	S7	5	52						5T, 07T	5T	5T		CH2	8A, 78A, 4, C-1A
r	C 1	CT.	C 1 A	F1			1			47	4 T	17 27	101	0111	14 4 04 704

#### **Control Table Generator Tool**

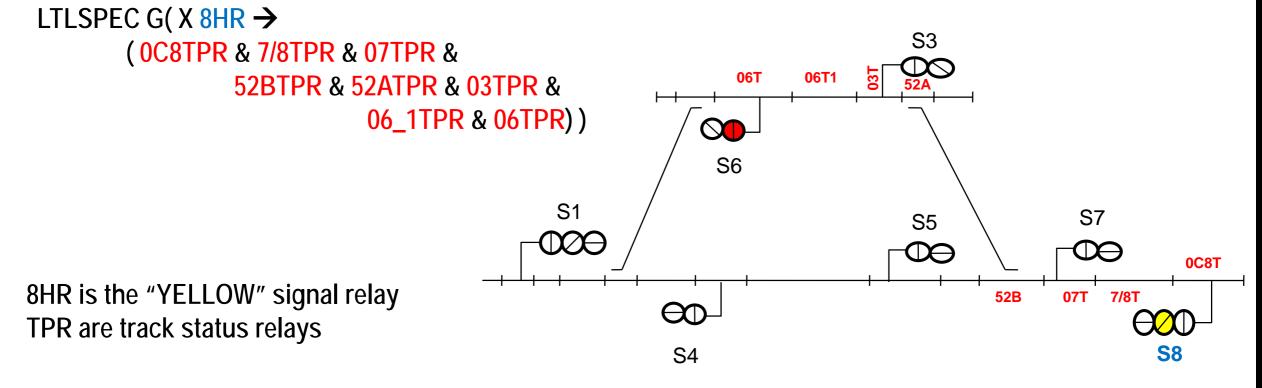
- Control table is automatically generated from the layout created by layout editor
- The tool checks for inherent inconsistencies
- Push-button solution whenever the layout is upgraded

### **IIT Kharagpur Contributions**

Example: Proving that the track circuits in the route up to the next signal and its overlap are clear. SafeR generates the following formal property.

#### The SafeR Tool

- Reads the control table
- Creates a comprehensive set of *formal properties*
- Built in knowledge about international railway signaling principles
- Thousands of properties are automatically verified using back-end formal tools



### **IIT-KGP EI Verification Tool Flow**

